

Operational Amplifiers

Prof. Dr. M. Zahurul Haq
zahurul@me.buet.ac.bd
<http://teacher.buet.ac.bd/zahurul/>

Department of Mechanical Engineering
Bangladesh University of Engineering & Technology

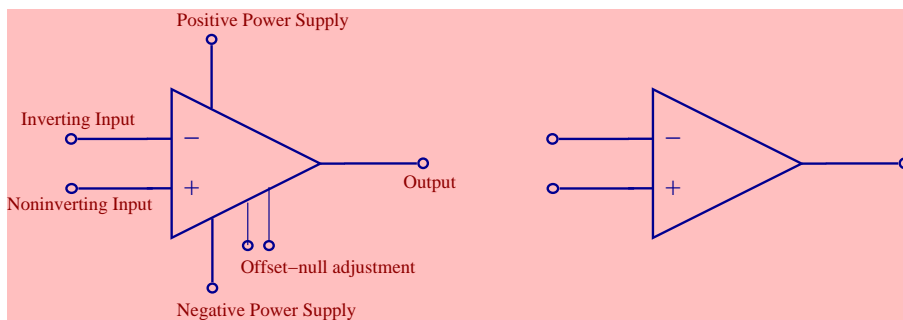
ME 361: Instrumentation & Measurement



OP-Amp: Components

The OP-Amp has **Single Output** and **Two Inputs**:

- 1 Noninverting input [+]: output is in phase with input.
- 2 Inverting input [-]: output is 180° out of phase with input.



x004.eps



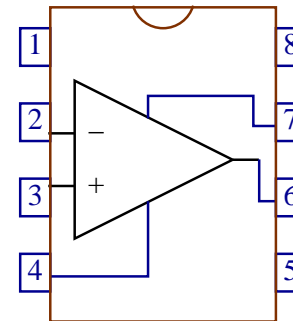
Operational Amplifier (Op-Amp)

The OP-Amp is a low-cost and versatile IC (Integrated Circuit) consisting of many internal transistors, resistors, and capacitors. These are basic building blocks for:

- Amplifiers
- Integrators and Differentiators
- Summers
- Comparators
- A/D and D/A converters
- Active filters
- Sample and Hold circuits
- ... etc.



LM 741: Pin Configuration



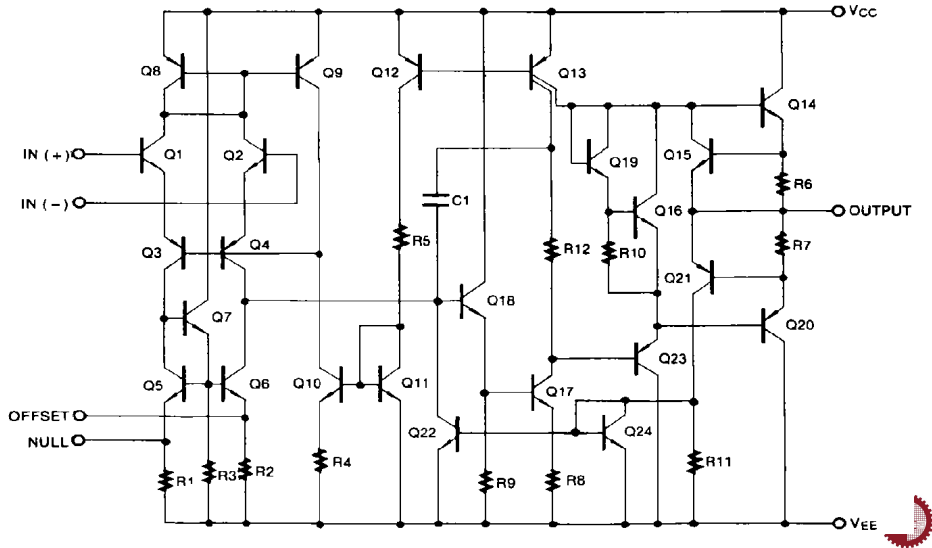
- 1 Offset Null
- 2 Inverting Input
- 3 Noninverting Input
- 4 -ve Power Supply
- 5 Offset Null
- 6 Output
- 7 +ve Power Supply
- 8 Not connected (N/C)

x005.eps

- LM 741 is the most widely used op-amp.
- A dot or notch at the end of the package identify the end to begin counting the pin numbers anti-clockwise.
- Offset null terminals enable corrections required for non-ideal behaviour of op-amps.



Internal Design of LM741



e039.eps

OP-Amp: Characteristics

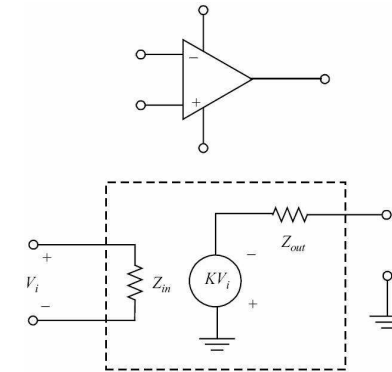
Characteristics	Ideal Value	Typical real-world value
Open-loop gain	∞	$10^5 V/V$
Offset voltage	0	$\pm 1 mV$
Bias currents	0	$10^{-6} - 10^{-14} A$
Input impedance	∞	$10^5 - 10^{11} \Omega$
Output impedance	0	$1 - 10 \Omega$

- Ideal op-amps rejects inputs common to both inputs (common mode rejection).
- Actual Common Mode Rejection Ratio, $CMRR = \frac{E_o/E_i}{E_o/E_{cm}} \geq 10^6$ the larger the CMRR, the better the amplifier.



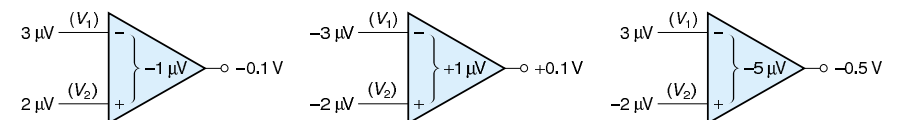
OP-Amp: Equivalent Circuit

- Rule 1. Infinite input impedance, $Z_{in} = \infty \Rightarrow I_+ = I_- = 0$;
- Rule 2. Infinite gain, $\Rightarrow E_+ = E_-$;
- Rule 3. Zero output impedance, $Z_{out} = 0 \Rightarrow E_o \neq f(I_o)$.

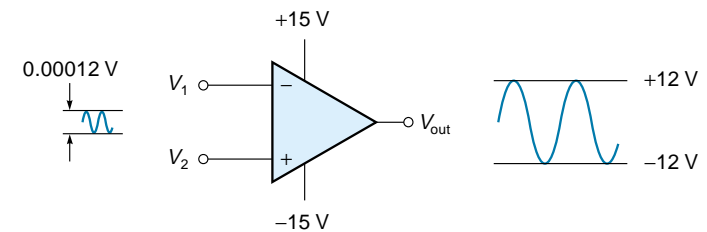


e427.eps

OP-Amp: Examples

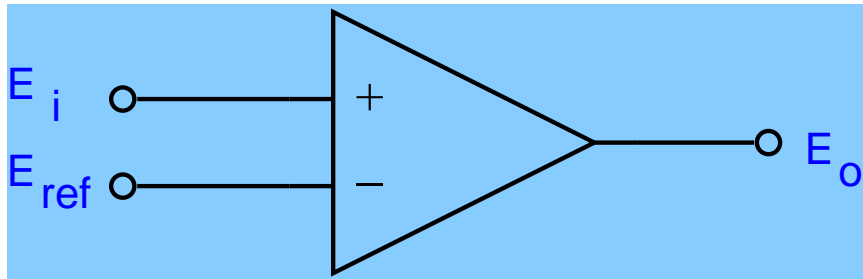


e176.eps



e177.eps

OP-Amp: Voltage Comparator



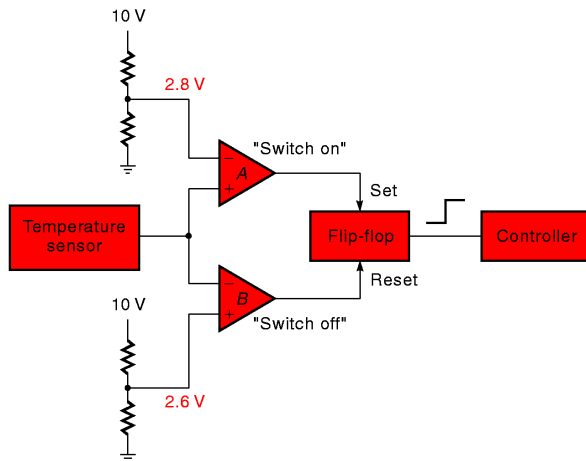
x007.eps

In comparator circuit, there is no negative feedback, hence the circuit exhibits infinite gain and the op-amps will saturate, i.e. the output remains at the most positive or most negative output value. Hence,

$$E_o = \begin{cases} +E_{sat} & E_i > E_{ref} \\ -E_{sat} & E_i < E_{ref} \end{cases}$$



Window Comparator Circuit

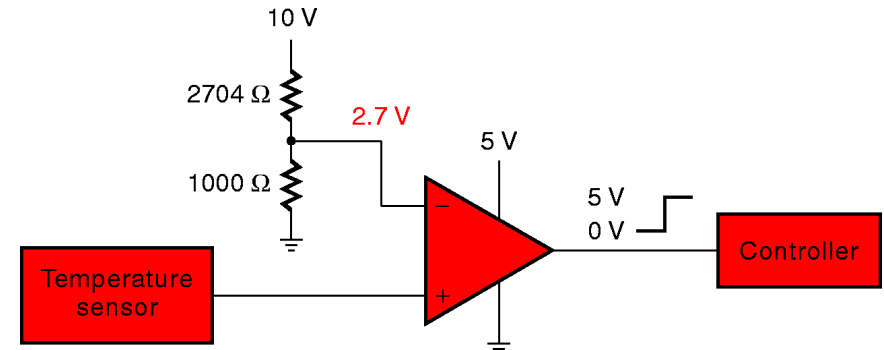


e041.eps

Window Comparator is with inbuilt hysteresis; hysteresis means that switch-on voltage is greater than switch-off voltage.



Comparator Circuit: Application

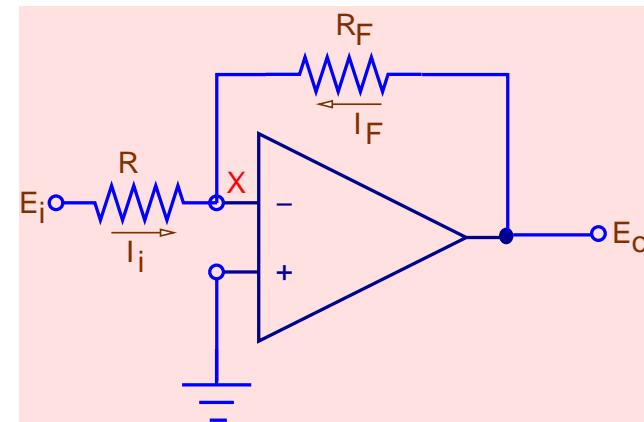


e040.eps

Chatter is a practical problem, output voltage oscillates back-and-forth when input voltage is near to the threshold.



OP-Amp: Inverting Amplifier

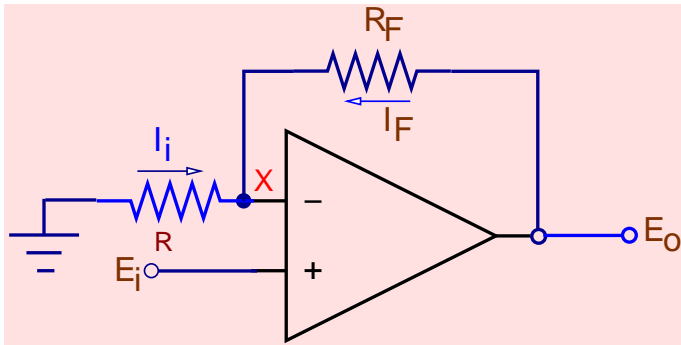


x008.eps

- At X, $I_i + I_F = 0$ (KCL & Rule 1), & $E_X = 0$ (Rule 2);
- $I_i \left(\equiv \frac{E_i - E_X}{R} \right) = -I_F \left(\equiv \frac{E_o - E_X}{R_F} \right) \implies$ gain, $G = \frac{E_o}{E_i} = -\frac{R_F}{R}$



OP-Amp: Noninverting Amplifier

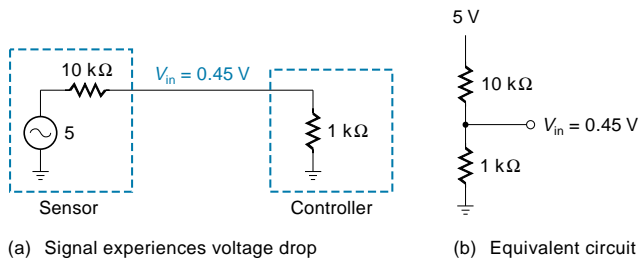


x009.eps

- At X, $I_i + I_F = 0$ (KCL & Rule 1), & $E_X = E_i$ (Rule 2);
- $I_i \left(\equiv \frac{-E_X}{R} \right) = -I_F \left(\equiv \frac{E_o - E_X}{R_F} \right) \Rightarrow G = 1 + \frac{R_F}{R}$

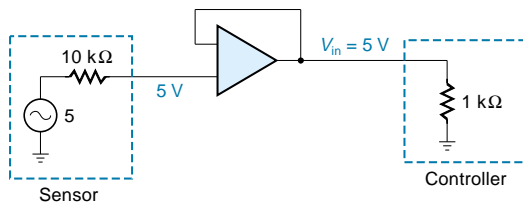


Op-Amp: Voltage Follower Application



(a) Signal experiences voltage drop

(b) Equivalent circuit



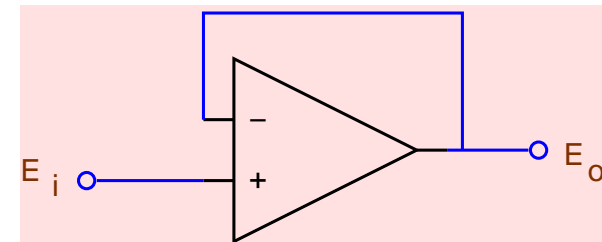
(c) No signal voltage drop

e178.eps



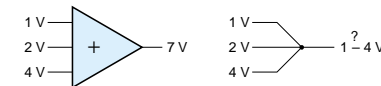
OP-Amp: Follower/Buffer

- In a noninverting amplifier with $R = \infty$ & $R_F = 0$, gain, G is unity and there is no voltage amplification. This circuit is known as a *buffer* or *follower*.
- It has a high input impedance and low output impedance. The high input impedance effectively isolates the source from the rest of the circuit.

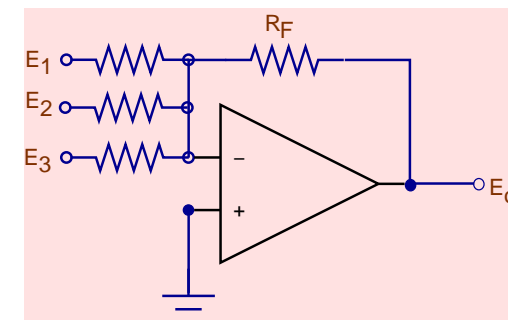


x010.eps

Op-Amp: Summing Amplifier



e179.eps



x011.eps

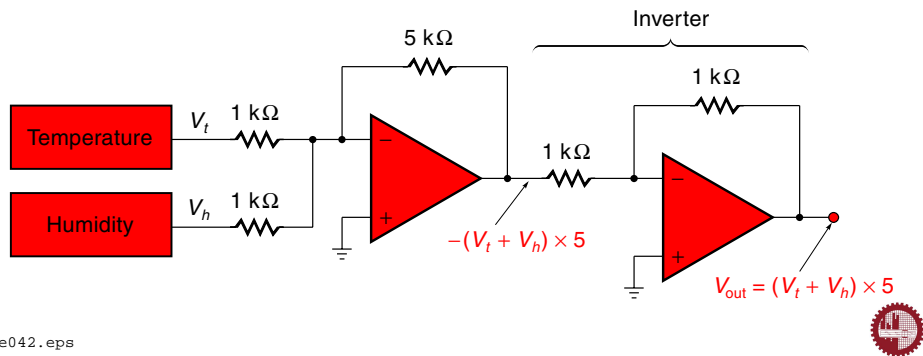
$$E_o = -R_F \left[\frac{E_1}{R_1} + \frac{E_2}{R_2} + \frac{E_3}{R_3} \right]$$



Summing Amplifier: Application

Example: Interface circuit for an air conditioning system

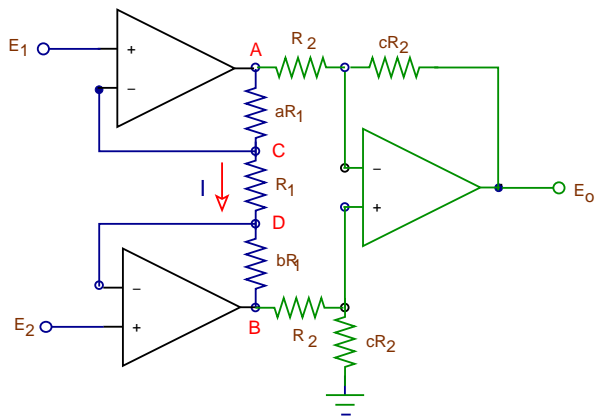
- when the sum of the voltages of temperature and humidity sensors goes above 1.0 V, &
- a threshold circuit in air conditioner require 5.0 V.



e042.eps



Instrument Amplifier



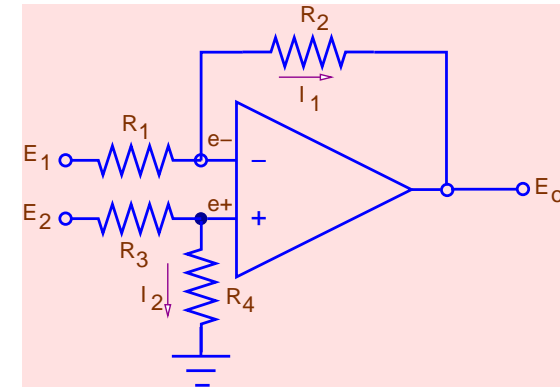
x013.eps

$$I = \frac{E_c - E_D}{R_1} = \frac{E_1 - E_2}{R_1} = \frac{E_A - E_B}{aR_1 + R_1 + bR_1}; \quad \& \quad E_o = c(E_A - E_B)$$

$$G = \frac{E_o}{E_2 - E_1} = c(1 + a + b)$$



OP-Amp: Differential Amplifier



x012.eps

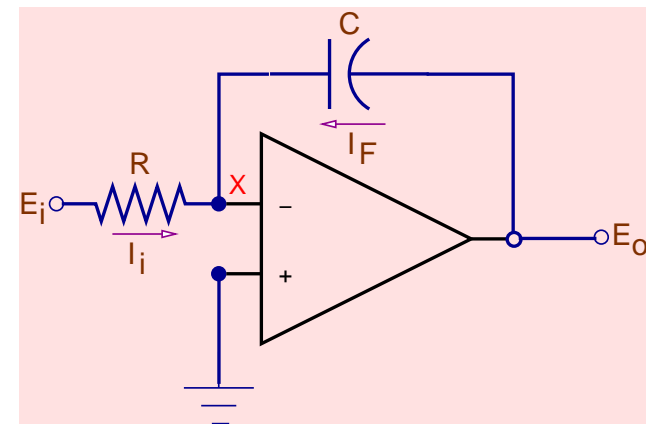
$$e^- = e^+ \Rightarrow E_1 \left[\frac{R_2}{R_1 + R_2} \right] + E_o \left[\frac{R_1}{R_1 + R_2} \right] = E_2 \left[\frac{R_4}{R_3 + R_4} \right]$$

$$E_o = E_2 \left[\frac{R_4}{R_3 + R_4} \cdot \frac{R_1 + R_2}{R_1} \right] - E_1 \left[\frac{R_2}{R_1} \right]$$

$$E_o = (E_2 - E_1) \left[\frac{R_2}{R_1} \right] = c(E_2 - E_1) \text{ if } \frac{R_2}{R_1} = \frac{R_4}{R_3} = c$$



OP-Amp: Integrator

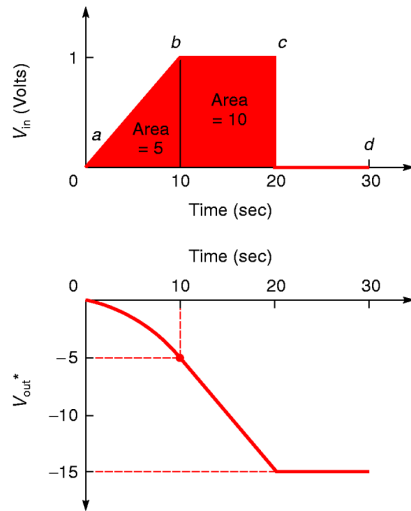


x014.eps

$$I_i = \frac{E_i}{R}, \quad I_F = C \frac{dE_o}{dt} \quad \& \quad I_i + I_F = 0 \text{ (KCL)}$$

$$E_o = -\frac{1}{RC} \int E_i(\tau) d\tau$$

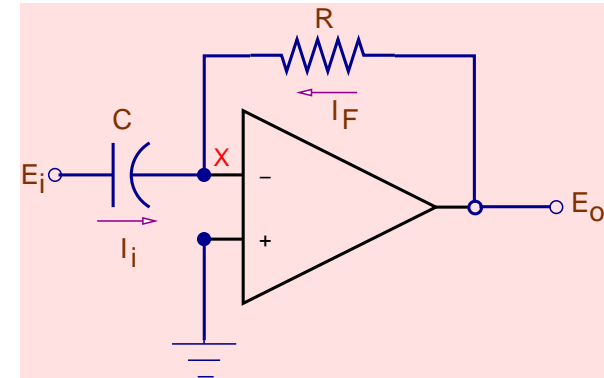


Output of an Integrator Circuit ($RC = 1$)

e043.eps



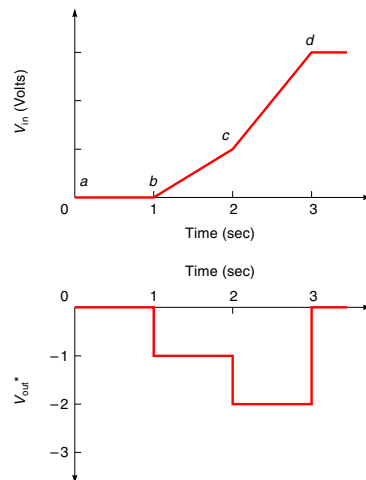
OP-Amp: Differentiator



x015.eps

$$I_i = C \frac{dE_i}{dt}, \quad I_F = \frac{E_o}{R} \quad \& \quad I_i + I_F = 0 \text{ (KCL)}$$

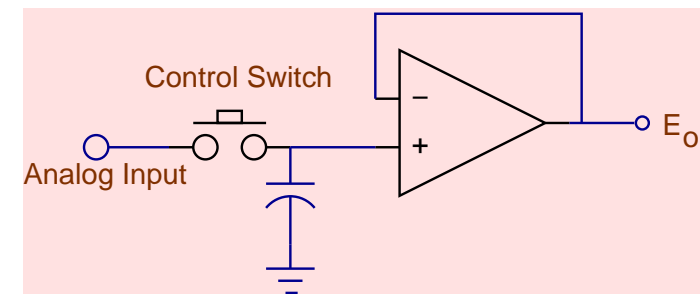
$$E_o = -RC \frac{dE_i}{dt}$$

Output of a Differentiator Ckt. ($RC = 1$)

e044.eps



OP-Amp: Sample and Hold Circuit



x016.eps

- S/H amplifier holds an analog value, until an A/D converter is ready to convert it to digital.
- The basis circuit consists of an electronic switch to the sample, with a capacitor for the hold and an op-amp voltage follower.

