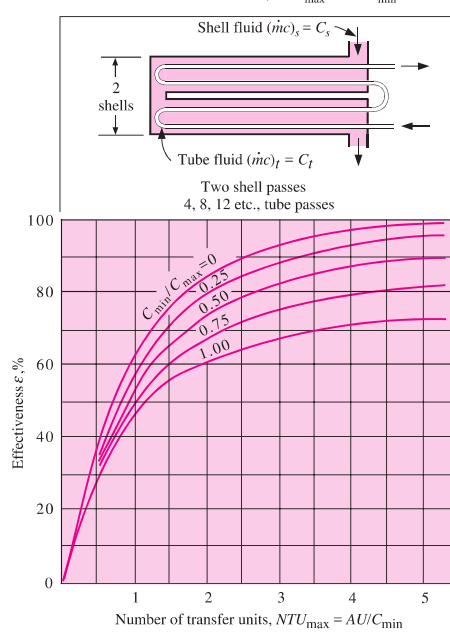
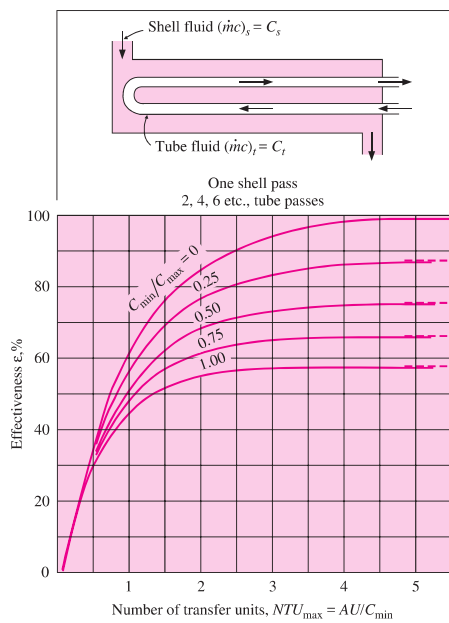
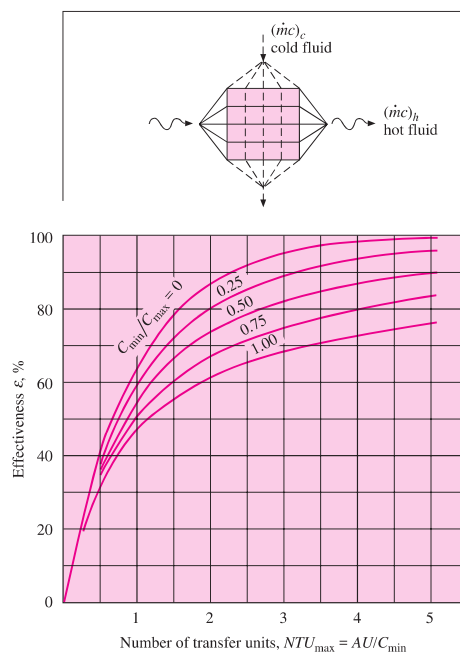
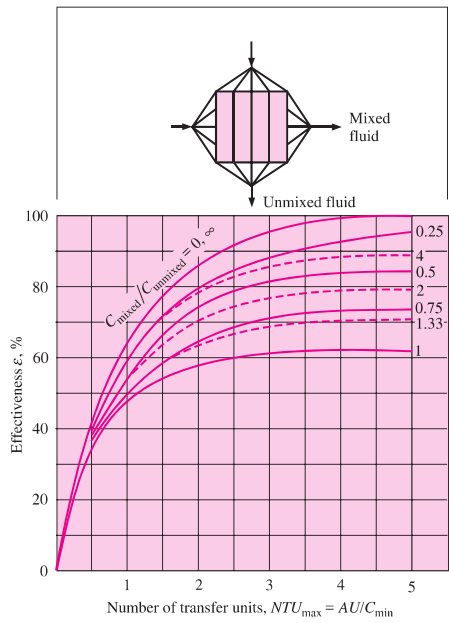
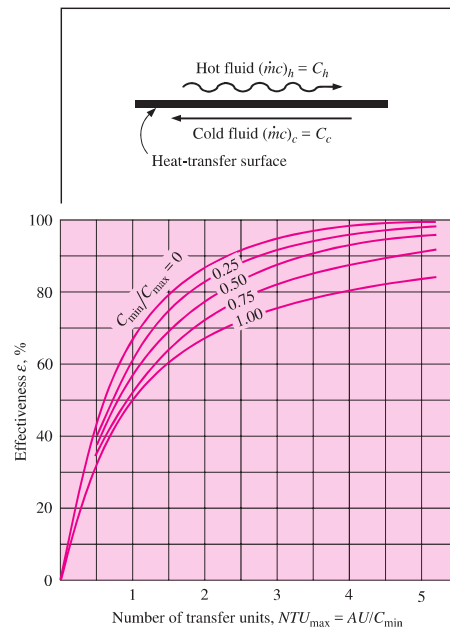
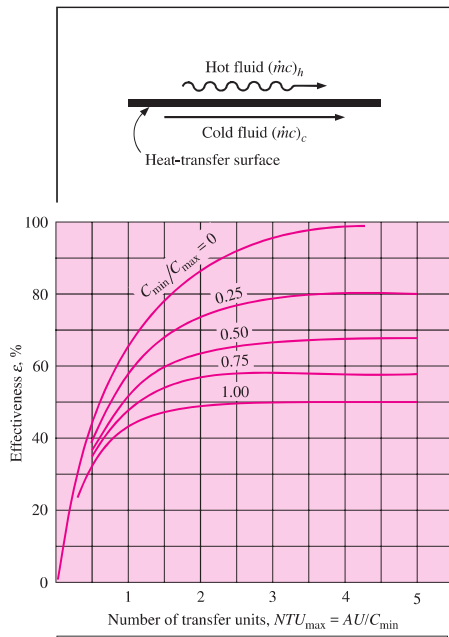
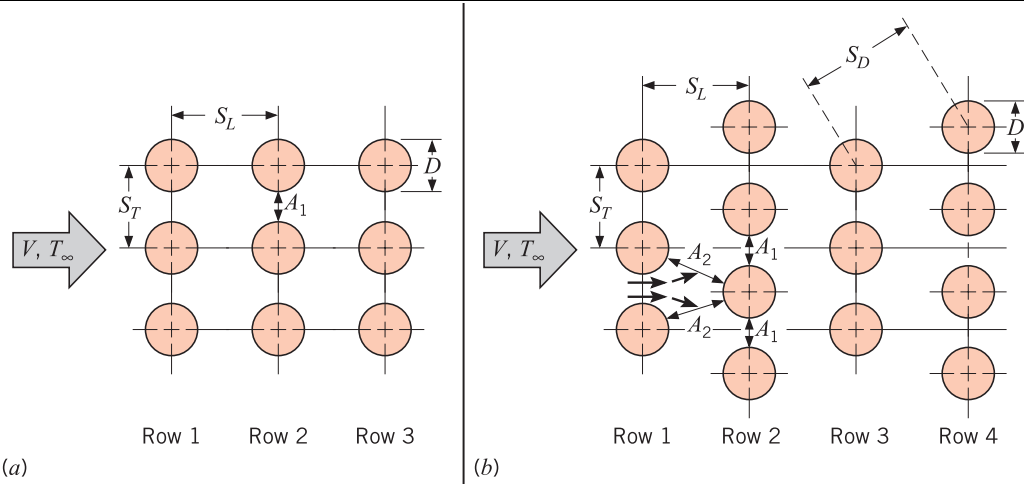


# ME 307: Heat Transfer Equipment Design



## Cross-Flow Heat Exchanger



- $Re_{D,max} = \frac{V_{max}D}{\nu}$

(a) In-line rows,  $V_{max} = u_{\infty} \left[ \frac{S_T}{S_T - D} \right]$

(b) Staggered row,  $V_{max} = \max \left( u_{\infty} \left[ \frac{S_T}{S_T - D} \right], u_{\infty} \left[ \frac{S_T}{2(S_D - D)} \right] \right)$ ,  $S_D = \sqrt{S_L^2 + (S_T/2)^2}$

- $Nu_m \equiv \frac{h_m D}{k} = C_1 Re_{D,max}^m Pr^{0.36} \left( \frac{Pr}{Pr_w} \right)^{1/4}$

Configuratio	$Re_{D,max}$	$C_1$	$m$
Aligned	$10-10^2$	0.80	0.40
Staggered	$10-10^2$	0.90	0.40
Aligned	$10^2-10^3$	Approximate as a single (isolated) cylinder	
Staggered	$10^2-10^3$		
Aligned ( $S_T/S_L > 0.7$ ) <sup>a</sup>	$10^3-2 \times 10^5$	0.27	0.63
Staggered ( $S_T/S_L < 2$ )	$10^3-2 \times 10^5$	$0.35(S_T/S_L)^{1/5}$	0.60
Staggered ( $S_T/S_L > 2$ )	$10^3-2 \times 10^5$	0.40	0.60
Aligned	$2 \times 10^5-2 \times 10^6$	0.021	0.84
Staggered	$2 \times 10^5-2 \times 10^6$	0.022	0.84

<sup>a</sup>For  $S_T/S_L < 0.7$ , heat transfer is inefficient and aligned tubes should not be used.

- $Nu_m|_{(N < 20)} = C_2 Nu_m|_{(N \geq 20)}$

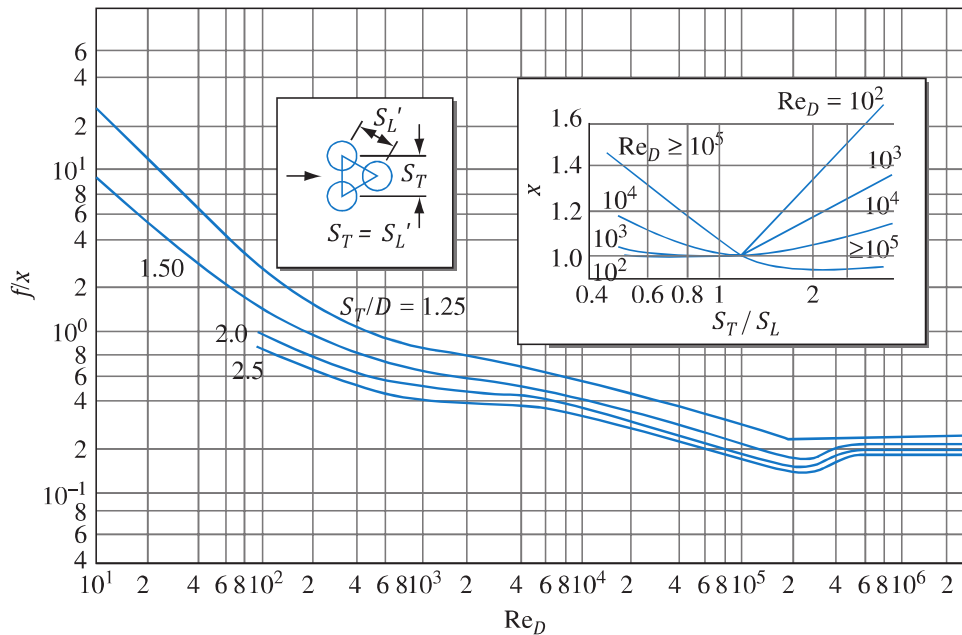
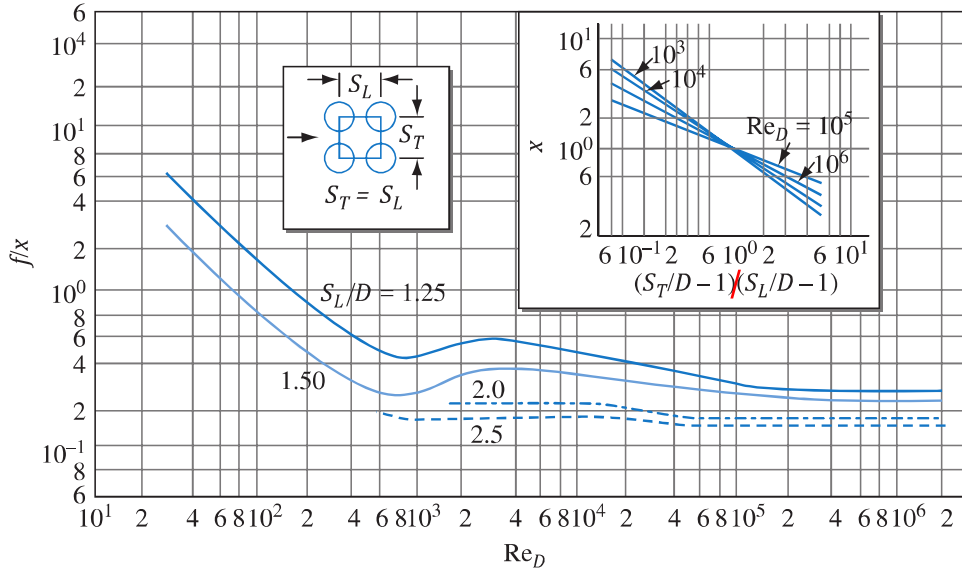
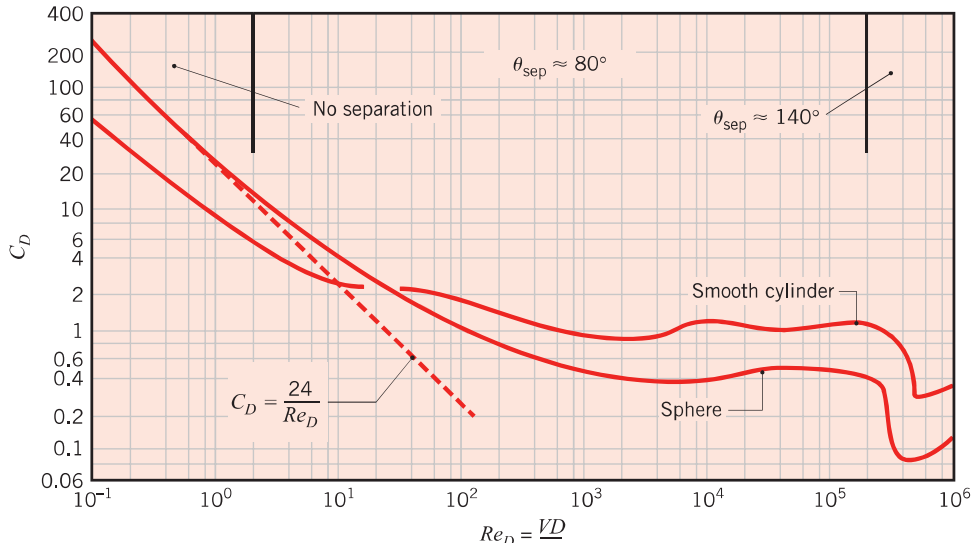
$N$	2	3	4	5	6	8	10	16	20
Staggered	0.77	0.84	0.89	0.92	0.94	0.97	0.98	0.99	1.0
In-line	0.70	0.80	0.90	0.92	0.94	0.97	0.98	0.99	1.0

- Pressure drop,  $\Delta P = f \left( \frac{1}{2} \rho V_{max}^2 \right) N_L$

- Pumping work,  $\dot{W}_p = \dot{V} \Delta P = V_{av} A \Delta P$

- Motor power,  $\dot{W}_{motor} = \frac{\dot{W}_p}{\eta_{pump}}$

$$F_D = C_D A \left( \frac{1}{2} \rho u_\infty^2 \right)$$



## Double Pipe Heat Exchanger

- Laminar:  $Nu = 1.86(Gz)^{1/3} \left( \frac{\mu_b}{\mu_w} \right)^{0.14}$ ;  $Gz = \frac{RePr}{L/D}$
- Turbulent:  $Nu = 0.023Re^{0.8}Pr^n$ ;  $n = \begin{cases} 0.4 & : \text{heating} \\ 0.3 & : \text{cooling} \end{cases}$
- Friction factor,  $f = \begin{cases} \xi_{corr} [64/Re] & : \text{laminar flow} \\ (1.82 \log_{10} Re - 1.64)^{-2} & : \text{turbulent flow} \end{cases}$

### Pipe area

- Equivalent diameter,  $De_p = Dh_p = ID_p$
- Pressure drop,  $\Delta P_p = f_p \frac{L}{ID_p} (\frac{1}{2} \rho_p V_p^2)$ ,  $\xi_{corr} = 1$

### Annular area

- $Dh_a = ID_a - OD_p$ ,  $De_a = \frac{ID_a^2 - OD_p^2}{OD_p}$
- $\frac{1}{\xi_{corr}} = \frac{1+\kappa^2}{(1-\kappa)^2} + \frac{1+\kappa}{(1-\kappa)\ln(\kappa)}$ ,  $\kappa = OD_p/ID_a$
- $\Delta P_a = (f_a \frac{L}{Dh_a} + 1) (\frac{1}{2} \rho_a V_a^2)$

## Shell & Tube Heat Exchanger

- Tube pitch ratio,  $PR \equiv P_T/OD_t$ ,  $1.2 \leq PR \leq 1.5$
- Preferred tube length,  $L$ :  
6 ft (1.83 m), 8 ft (2.44 m), 12 ft (3.66 m), 16 ft (4.88 m), 20 ft (6.1 m), 24 ft (7.32 m).
- Total outside tube area,  $A_o = N_t(\pi OD_t L)$
- $CL = \begin{cases} 1.0 & \text{for } 90^\circ, 45^\circ \\ 0.87 & \text{for } 30^\circ, 60^\circ \end{cases}$
- $CTP = \begin{cases} 0.93 & : 1 \text{ tube - pass} \\ 0.90 & : 2 \text{ tube - passes} \\ 0.85 & : 3 \text{ tube - passes} \end{cases}$
- Shell inside diameter,  $D_s = 0.637 \sqrt{\frac{CL}{CTP} \left[ \frac{A_o(PR)^2 OD_t}{L} \right]^{1/2}}$

### Tube-side

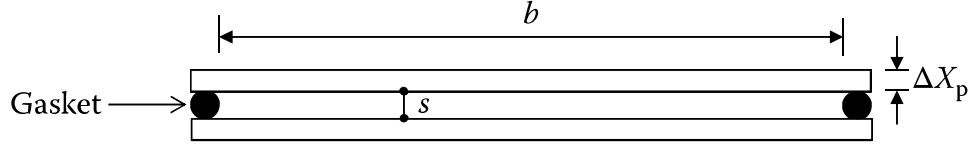
- Total tube x-section area,  $A_t = \left( \frac{N_t}{N_p} \right) \frac{\pi}{4} ID_t^2$   $N_p = \text{no. of pass}$
- Laminar:  $Nu = 1.86(Gz)^{1/3} \left( \frac{\mu_b}{\mu_w} \right)^{0.14}$ ;  $Gz = \frac{RePr}{L/OD_t}$
- Turbulent:  $Nu = 0.023Re^{0.8}Pr^n$ ;  $n = \begin{cases} 0.4 & : \text{heating} \\ 0.3 & : \text{cooling} \end{cases}$
- For smooth pipes,  $f_t = \begin{cases} 0.316Re^{-0.25} & : Re \leq 2 \times 10^4 \\ 0.184Re^{-0.20} & : 2 \times 10^4 \leq Re \leq 3 \times 10^5 \end{cases}$
- Pressure drop,  $\Delta P_t = N_p \left( f_t \frac{L}{ID_t} + 4 \right) (\frac{1}{2} \rho_t V_t^2)$

### Shell-side

$$Dh_s = \frac{4A}{P} = \begin{cases} \frac{4P_T^2}{\pi OD_t} - OD_t & : \text{square pitch} \\ \frac{2\sqrt{3}P_T^2}{\pi OD_t} - OD_t & : \text{triangular pitch} \end{cases}$$

- $0.4D_s \leq B \leq 0.6D_s$ ,  $B = \text{baffle spacing}$ , Number of baffles,  $N_b = \frac{L}{B} - 1$
- Bundle cross-flow area,  $A_s = \frac{D_s CB}{P_T}$
- $Nu = 0.36Re_s^{0.55}Pr^{1/3}$ ,  $Re_s = V_s Dh_s / \nu_s$
- $f_s = \exp[0.576 - 0.19 \ln(Re_s)]$
- $\Delta P_s = f_s (N_b + 1) \frac{D_s}{D_e} (\frac{1}{2} \rho_s V_s^2)$

Plate & Frame Heat Exchanger



- $NTU = \frac{U_o A_o N_s}{(\dot{m} C_p)_{min}}$ ,  $A_o = bl$
- Effective  $NTU = F_{corr} NTU$ ,  $F_{corr} = 1 - 0.0166 NTU$
- $\frac{1}{U_o} = \frac{1}{h_h} + \frac{1}{h_c} + \frac{\Delta X_p}{k} + R_{di} + R_{do}$
- Flow velocity,  $V = \begin{cases} \frac{2\dot{m}}{\rho s b (N_s + 1)} & : \text{odd number of plates} \\ \frac{2\dot{m}}{\rho s b N_s}, \frac{2\dot{m}}{\rho s b (N_s + 2)} & : \text{even number of plates} \end{cases}$
- $D_h = \frac{4(\text{cross-sectional area})}{\text{wetted perimeter}} = \frac{4sb}{2s+2b} \simeq \frac{4sb}{2b} = 2s$ ,  $Re = \frac{VD_h}{\nu}$
- Laminar flow:  $Nu = 1.86(Gz)^{1/3} \left(\frac{\mu_b}{\mu_w}\right)^{0.14}$ ;  $Gz = \frac{RePr}{L/D}$   $Re < 100$
- Turbulent flow:  $Nu = 0.374 Re^{0.668} Pr^{1/3}$ ;  $Re > 100$
- Friction factor,  $f = \begin{cases} \frac{280}{Re} & : 1 < Re < 10 \\ \frac{100}{Re^{0.589}} & : 10 < Re < 100 \\ \frac{12}{Re^{0.183}} & : Re > 100 \end{cases}$
- Pressure drop,  $\Delta P = \frac{fL}{D_h} \left(\frac{1}{2}\rho V^2\right) + 1.3\left(\frac{1}{2}\rho V_p^2\right) \simeq \frac{fL}{D_h} \left(\frac{1}{2}\rho V^2\right)$

Condensation Correlations

- Condensation on vertical surfaces

$$h_m = 1.2 \times 0.943 \left[ \frac{g\rho_l(\rho_l - \rho_v)h_{fg}k_l^3}{\mu_l(T_v - T_w)L} \right]^{1/4}$$

- Condensation on inclined surfaces

$$h_m = 0.943 \left[ \frac{g\rho_l(\rho_l - \rho_v)h_{fg}k_l^3}{\mu_l(T_v - T_w)L} \sin\varphi \right]^{1/4}$$

- Condensation on horizontal tube

$$h_m = 0.725 \left[ \frac{g\rho_l(\rho_l - \rho_v)h_{fg}k_l^3}{\mu_l(T_v - T_w)D} \right]^{1/4}$$

- Condensation on horizontal tube banks

$$h_m|_{N \text{ tubes}} = \frac{1}{N^{1/4}} h_m|_{1 \text{ tube}}$$

- Condensation inside horizontal tube

$$h_m = 0.555 \left[ \frac{g\rho_l(\rho_l - \rho_v)h'_{fg}k_l^3}{\mu_l(T_v - T_w)D} \right]^{1/4}$$